Timing and Clocking

6.205

Planning Stuff

- Week 03 Due Tomorrow
- Week 04 Released Thursday (video)

Look at your Vivado logs!

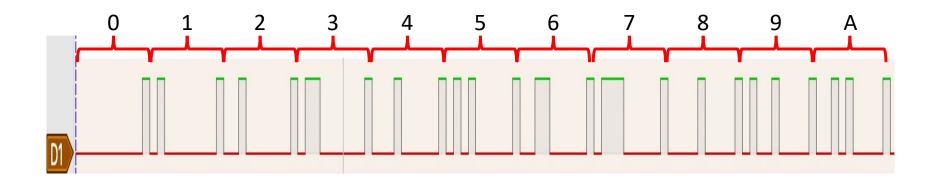
- If your build doesn't work, open up the obj folder and the vivado.log file will have information about your build.
- Go through it! Focus on Warnings and Critical Warnings,
 - "latch"....not good.
 - "multi-driven net"....not good.
 - "no driver"...possibly not good if referring to signal you care about.
 - "no load"...possibly not good if referring to signal you care about.

Look at your Vivado logs!



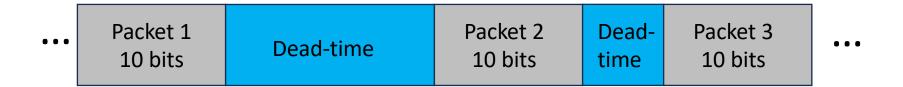
Notes on UART RX

- I went and from the computer decided to send down 0, then 1, then 2, then 3...to 255 over UART.
- This was the trace on the UART_RXD line



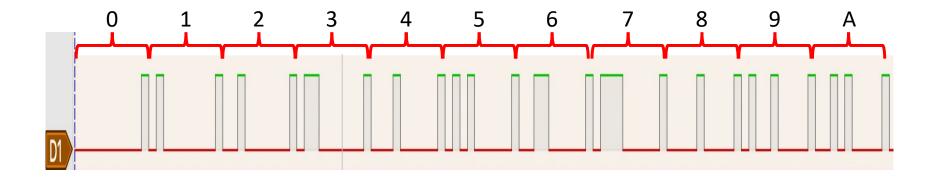
UART Packet

- In the UART standard there is no guarantee in regards to inter-byte spacing between bytes sent down.
- It can vary (and often does)



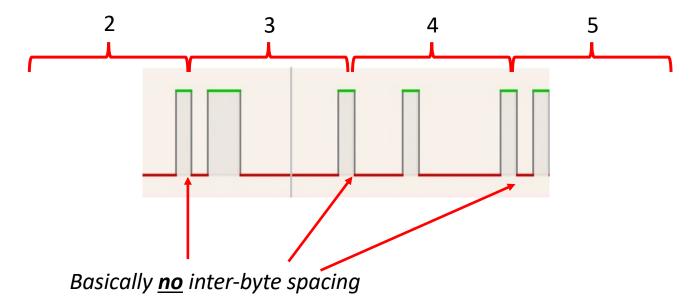
However...the FT2232 chip on our board that handles the UART...

Packs the UART packets very tightly



However...the FT2232 chip on our board that handles the UART...

Packs the UART packets very tightly

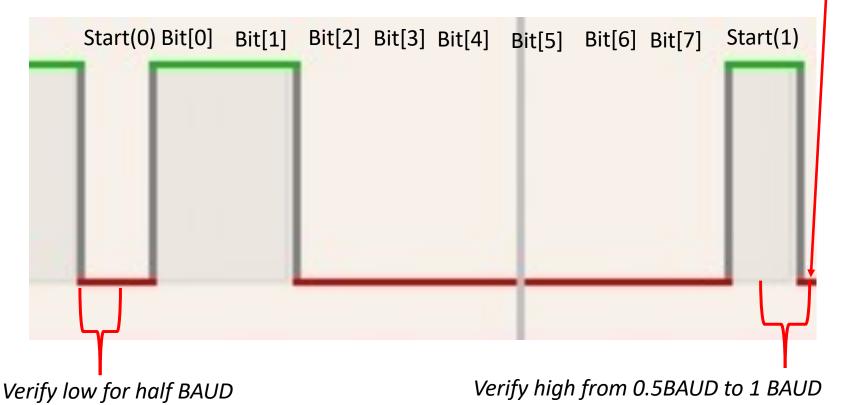


As a result...

9/23/25

Could fall off cliff into next start bit...:/

 Be careful with verifying too long or staying in a state too long! Read instructions for uart_receive!



FSMs in History

Car Alarm FSM

 Up until 2021 the "FSM" lab in 6.111 was making a car alarm

 FSM design was and still can be a very common approach to digital circuit design



»Lectures »Labs: 1, 2, 3, 4, 5A

Final Projects

»Project info

»Project list

Since your client is completely focused on her start-up, she wants an anti-theft system that's highly automated. The system is armed automatically after she turns off the is ssenger and both the driver's door and passenger's doors are open, the system arms itself after all the doors have been closed and T_ARM_DELAY has passed; that dela

Once the system has been armed, opening the driver's door the system begins a countdown. If the ignition is not turned on within the countdown interval (T. DRIVER, D. T_ALARM_ON) after the door closes, at which time the system resets to the armed but silent state. If the ignition is turned on within the countdown interval, the system

Always a paragon of politeness, your client opens the passenger door first if she's transporting a guest. When the passenger door is opened first, a separate, presumably

There is a status indicator LED on the dash. It blinks with a two-second period when the system is armed. It is constantly illuminated either the system is in the countdov

So far this all is ordinary alarm functionality. But you're worried that a knowledgable thief might disable the siren and then just drive off with the car. So you've added an Power is only restored when first the ignition is turned on and then the driver presses both a hidden switch and the brake pedal simultaneously. Power is then latched on u

The diagram below lists all the sensors (inputs) and actuators (outputs) connected to the system

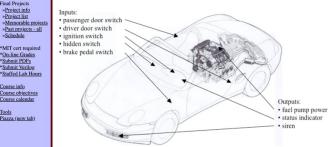


Figure 1: System diagram showing sensors (inputs) and actuators (outputs)

The system timings are based on four parameters (in seconds): the delay between exiting the car and the arming of the alarm (T_ARM_DELAY), the length of the countd (T_PASSENGER_DELAY), and the length of time the siren sounds (T_ALARM_ON). The default value for each parameter is listed in the table below, but each may be Time_Parameter_Selector switches specify the parameter number of the parameter to be changed. Time_Value switches are a 4-bit value representing the value to be prog selected parameter to Time_Value. Note that your system should behave correctly even if one or more of the parameters is set to 0.

Default Timing Parameters										
Interval Name	Symbol	Parameter Number	Default Time (sec)	Time Value						
Arming delay	T_ARM_DELAY	00	6	0110						
Countdown, driver's door	T_DRIVER_DELAY	01	8	1000						
Countdown, passenger door	T_PASSENGER_DELAY	10	15	1111						
Siren ON time	T_ALARM_ON	11	10	1010						

Block Descriptions/Implementation

The following diagram illustrates a possible organization of your design into modules



Car Alarm FSM

- When Gim graduated from MIT he got a job with DEC (Digital Equipment Corporation) that made the PDP-1 among other computers and then TI
- Got big signing bonus and bought a nice convertible
- Parked Convertible went into apartment.
- Convertible was not there came out



Gim Hom Took 6.111 in 1969..graduated in 1970 6.111 Instructor 2013-2021 Now retired

Car Theft FSMs

• 2016, MA: ~7 million people, 6,600 car thefts for year

• 1975, MA: 5.8 million people, 91,000 car thefts for year (peak)

Mas	ssach	usetts Po	pulation	on and	Rate of	Crime	Rank	Comp	ared to	other S	tates	
State	Year	Population	Index	Violent	Property	Murder	Rape	Robbery	Assault	Burglary	Larceny	Vehicle
Massachusetts	1960	8	35	36	33	41	38	32	36	34	38	11
Massachusetts	1961	8	29	35	28	42	35	31	34	29	32	7
Massachusetts	1962	9	26	33	24	40	37	25	31	26	31	7
Massachusetts	1963	9	28	33	27	40	39	27	33	27	33	4
Massachusetts	1964	9	26	33	25	37	37	24	38	25	34	2
Massachusetts	1965	10	23	33	22	36	39	21	36	23	35	1
Massachusetts	1966	10	24	32	23	38	41	19	36	21	37	1
Massachusetts	1967	10	25	34	25	38	37	23	37	25	38	1
Massachusetts	1968	10	21	31	20	35	35	21	35	19	35	1
Massachusetts	1969	10	19	29	18	35	38	19	35	15	34	1
State	State Year Population Index Violent Property Murder Rape Robbery Assault Burglary Larceny Vehicle											
Massachusetts	1970	10	20	31	18	38	33	19	35	14	35	1
Massachusetts	1971	10	16	27	16	36	38	13	33	13	32	1
Massachusetts	1972	10	17	26	16	38	39	11	29	13	35	1
Massachusetts	1973	10	15	20	14	36	34	10	29	12	33	1
Massachusetts	1974	10	12	20	11	37	37	10	29	12	32	1
Massachusetts	1975	10	11	16	12	39	29	9	26	13	34	1
Massachusetts	1976	10	13	18	12	40	37	11	22	11	36	1
Massachusetts	1977	10	15	17	16	43	31	12	19	13	37	1
Massachusetts	1978	10	16	16	17	40	31	13	19	12	38	1
Massachusetts	1979	10	16	15	15	41	32	12	16	11	36	1
State Year Population Index Violent Property Murder Rape Robbery Assault Burglary Larceny Vehicle												
Massachusetts	1980	11	16	13	17	39	31	9	13	13	39	1
Massachusetts	1981	11	20	12	21	40	30	8	15	17	40	1
Massachusetts	1982	11	18	14	21	37	31	10	13	19	40	1
Massachusetts	1983	11	20	12	22	40	28	9	10	20	41	1
Massachusetts	1984	12	25	13	24	36	25	12	12	25	41	2
Massachusetts	1985	12	23	16	25	39	23	12	14	24	40	1
Massachusetts	1986	12	26	18	27	38	26	14	17	28	43	1
Massachusetts	1987	13	26	14	28	42	26	15	14	31	45	1
Massachusetts	1988	13	23	13	25	38	25	14	11	29	41	3

~5% of cars were stolen per year in MA

Massachusetts was the #1 state for car theft for 1965-1987!!!

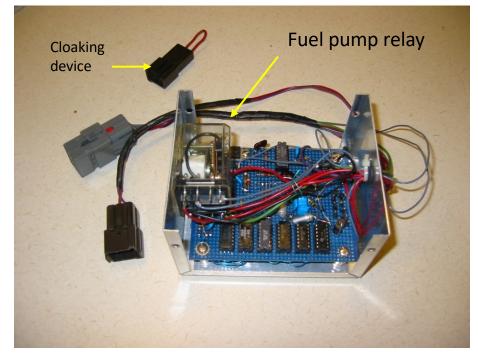
State	Year	Population	Index	Violent	Property	Murder	Rape	Robbery	Assault	Burglary	Larceny	Vehicle
Massachusetts	2000	13	42	21	44	41	36	27	14	41	49	16
Massachusetts	2001	13	41	20	43	42	29	25	15	40	47	18
Massachusetts	2002	13	39	18	42	38	34	24	17	39	46	18
Massachusetts	2003	13	28	17	40	42	30	19	18	36	46	18
Massachusetts	2004	13	39	18	42	37	33	20	18	38	47	22
Massachusetts	2005	13	42	19	45	37	36	20	18	35	48	30
Massachusetts	2006	13	41	20	44	35	37	21	19	34	45	33
Massachusetts	2007	14	42	22	42	37	38	23	18	33	45	36
Massachusetts	2008	14	37	20	44	41	39	24	14	32	45	35
Massachusetts	2009	15	37	17	43	38	38	23	14	33	45	33
State	Year	Population	Index	Violent	Property	Murder	Rape	Robbery	Assault	Burglary	Larceny	Vehicle
Massachusetts	2010	14	32	13	38	31	35	18	11	29	41	34
Massachusetts	2011	14	36	14	42	37	37	20	12	32	43	34
Massachusetts	2012	14	40	19	44	46	39	20	14	33	48	39
Massachusetts	2013	14	36	16	45	43	16	18	15	35	46	39
Massachusetts	2014	14	39	18	46	43	35	20	14	38	47	40
Massachusetts	2015	15	42	18	47	45	38	27	14	42	48	42
Massachusetts	2016	15	45	23	47	47	42	26	20	45	49	44

Car Alarm FSM

- Gim built a car alarm for his car.
- Designed it using an FSMbased approach.
- Had ~11 states
- Built it just like we talked about last week (bubblediagram...developed logic, implemented...)



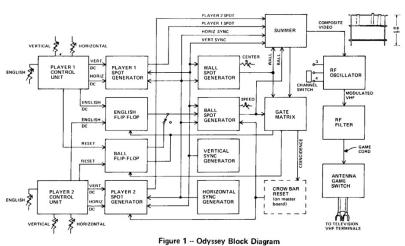
Gim's FSM-based car alarm for his car Built using 4000-series CMOS chips (top of the line at the time)

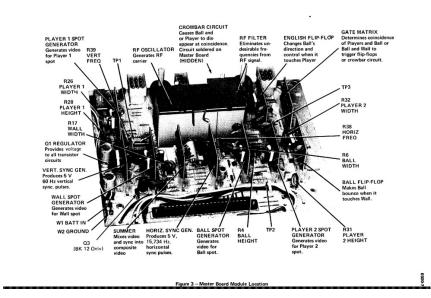


Magnavox Odyssey (1972)

- First commercially available game system
- Completely FSM-based

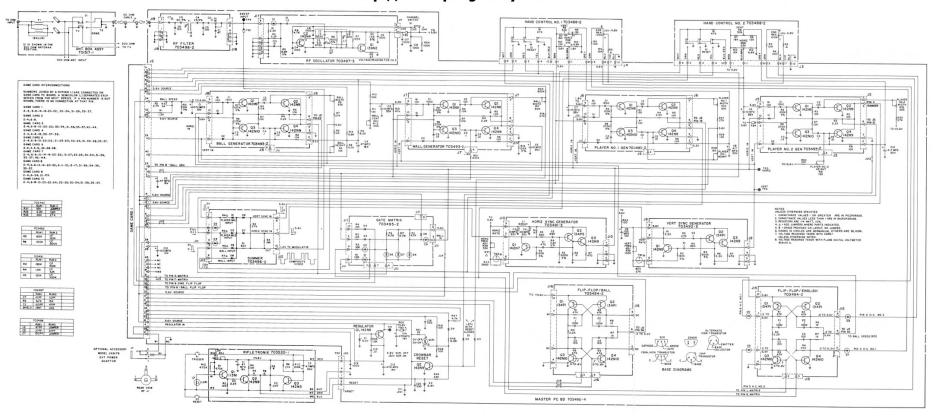






• Implemented completely with discrete transistors:

MAGNAVOX ODYSSEY 1TL200BLAK SCHEMATIC DIAGRAM Scanned from original service manual by David WINTER http://www.pong-story.com



Was just a large finite state machine

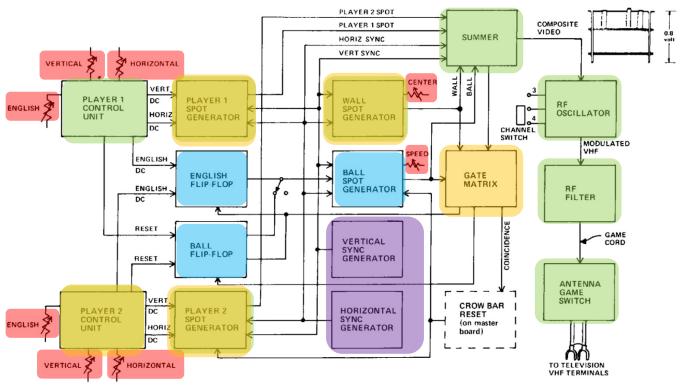
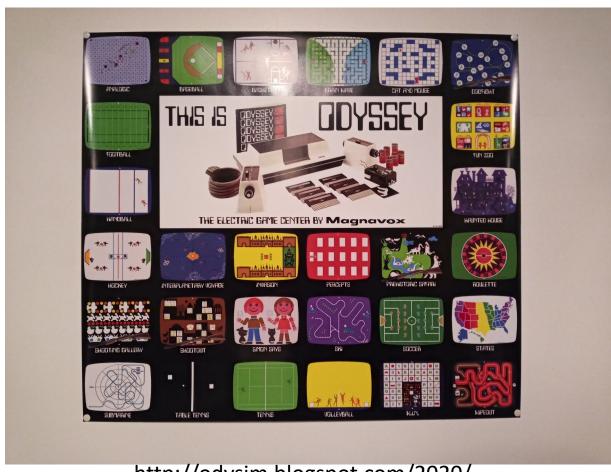


Figure 1 -- Odyssey Block Diagram



Magnavox Odyssey Game System



http://odysim.blogspot.com/2020/

Magnavox Odyssey Game System

Hockey



Basketball



Cat and Mouse



19

https://youtube.com/playlist?list=PLtApm-Ri5WTIAEV1ClufPrca2MTj4uSvT&feature=shared https://www.youtube.com/watch?app=desktop&v=NsluZfTMRno&ab_channel=OdysseyNow

Early 1970s

- Most arcade systems were just FSMs implemented in discrete logic, including:
 - Pong
 - Breakout
- Space Invaders was first arcade machine to move some game logic to an Intel 8080 microprocessor.

Evolution of FSM-based Games

- As 1970s rolled on, entire game systems would get put on single chips
- "Ball-and-Paddle" Chips would be sold by companies and then other companies would buy them and put their own "skin" on them and sell them as their own. Many times it was the same game underneath
- Atari 2600 was first microprocessor-based home video game system



AY-3-8500 "Ball-and-Paddle" chip

http://www.pong-story.com/gi.htm

TV Fun



- Runs off an AY-3-8500
- Made by APF who started out importing Japanese
 8-track players
- Company went bankrupt in the great video game crash of 1983.
- Have one set upstairs in lab in case anybody wants to play.

Tiger Electronics Games





Tiger Electronics Games

- Tiger Electronics had 100's of versions of these in the 1980s and 1990s
- Almost all of them were based on three or four common finite state machine game chips or four-bit microcontrollers (very poorly documented/insider information)
- They'd slap a different LCD skin and game art onto the same chip and resell









Modern Games

 Modern games are far too complex to be implemented with an FSM in any productive way (though it is still generally possible)

 However well-characterized chunks of game software is still used and re-used/skinned (for example game engines)

But also stuff gets reskinned all the time

Candy Crush Saga





Pet Rescue Saga





Soda Saga



Bubble Witch 3 Saga



9/23/25

https://fpga.mit.edu/6205/F25

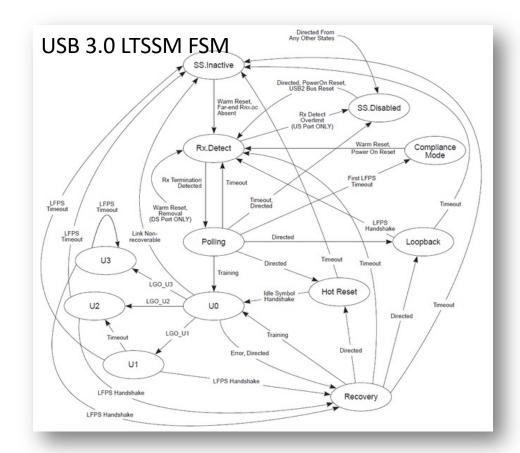
Farm Heroes Saga

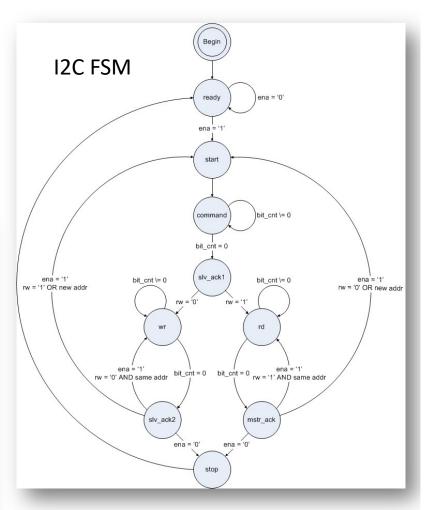


Finite State Machines Relevant

- Designing systems as finite state machines is still very common in digital design.
- Doing it in a structured way can make your HDL very transparent so you know what you're getting!
- You'll see data sheets and other places with FSM diagrams and many protocols express their functionality with FSMs.

See them everywhere

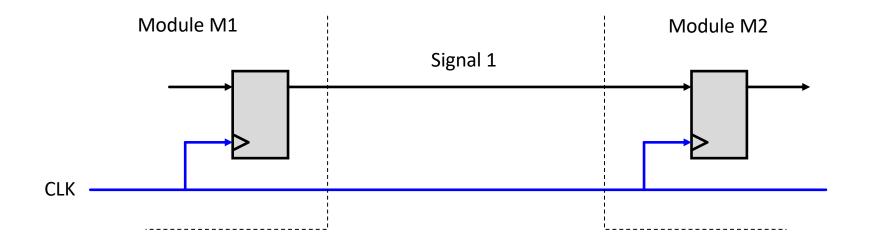




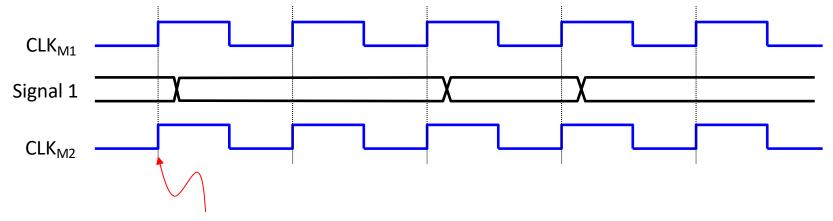
Clocks and Time

Times and Clocks

Clocking and Synchronous Communication

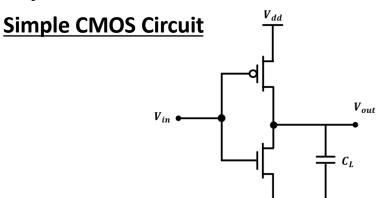


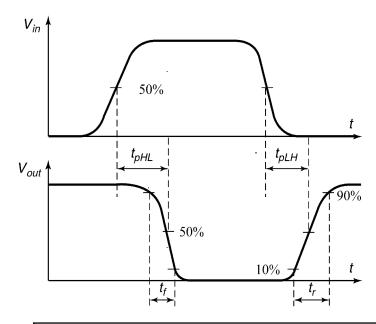
Ideal world:



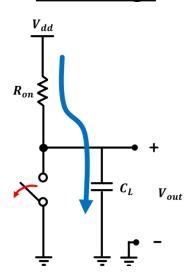
M1 and M2 clock edges aligned in time

Delay Estimation: Simple RC Networks

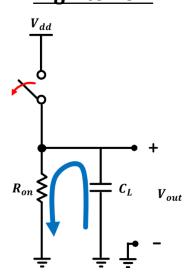




Low-to-High

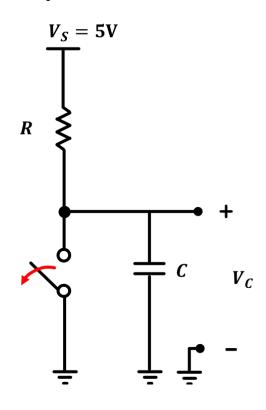


High-to-Low



review
$$V_{out}$$
 V_{out}
 V_{out}

RC Equation



$$V_c = 5 \left(1 - e^{-\frac{t}{RC}} \right)$$

$$V_s = 5 V$$

Switch is closed t<0

Switch opens t>0

$$V_{s} = V_{R} + V_{C}$$

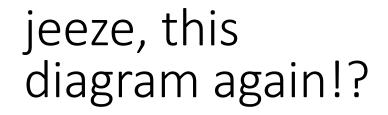
$$V_{s} = i_{R}R + V_{c} \quad i_{R} = C\frac{dV_{c}}{dt}$$

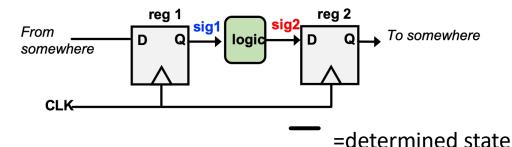
$$V_{s} = RC\frac{dV_{c}}{dt} + V_{c}$$

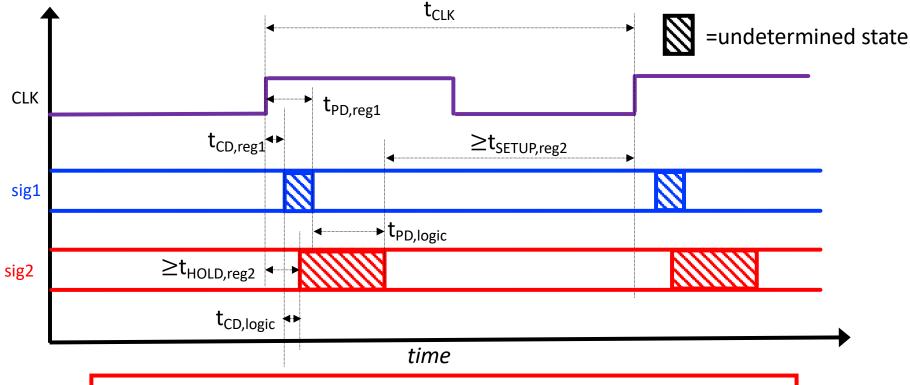
$$V_c = V_s \left(1 - e^{-\frac{t}{RC}} \right)$$

So Signals Experience Delays

- "Signals" generally have their delays expressed with:
 - Contamination Delay
 - Propagation Delay
- But the clock is not immune to delay too!



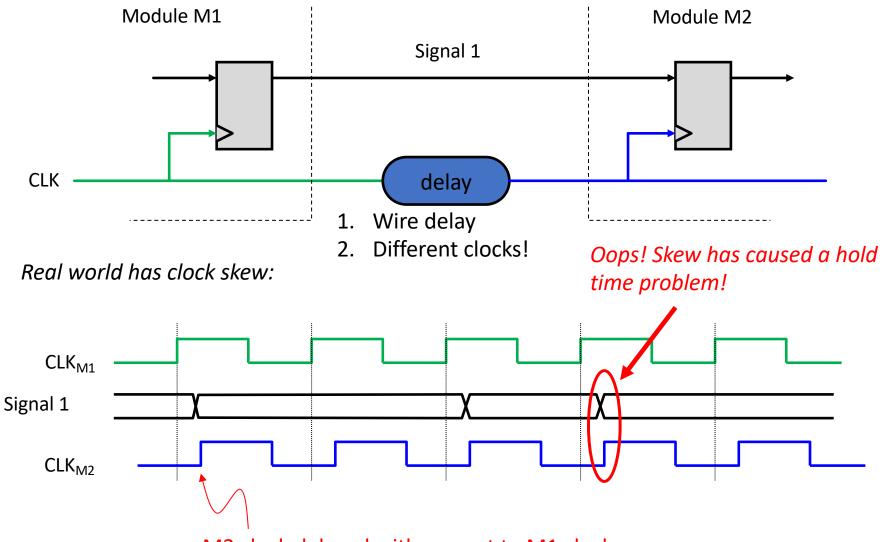




Two Requirements/Conclusions:

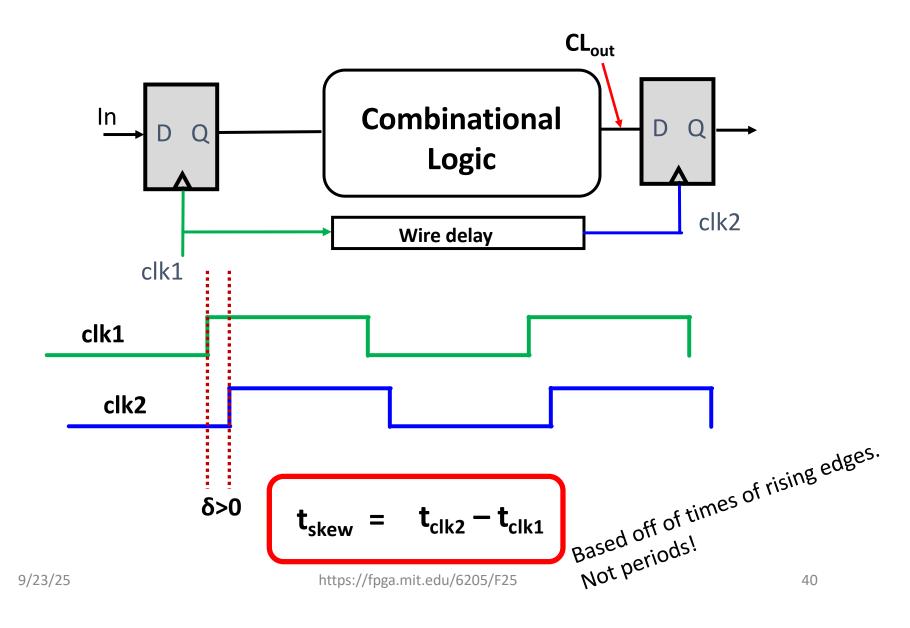
$$\begin{aligned} t_{\text{PD,reg1}} + t_{\text{PD,logic}} + t_{\text{SETUP,reg2}} &\leq t_{\text{CLK}} \\ t_{\text{CD,reg1}} + t_{\text{CD,logic}} &\geq t_{\text{HOLD,reg2}} \end{aligned}$$

Clock Skew

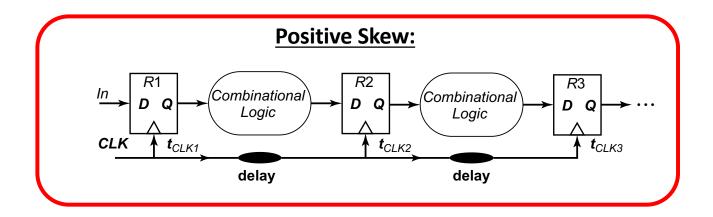


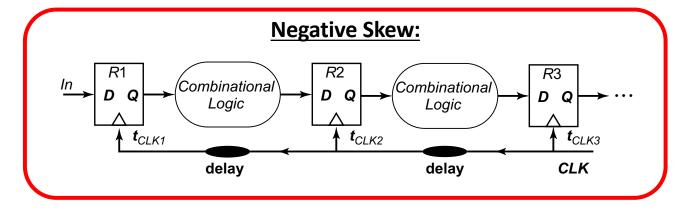
M2 clock delayed with respect to M1 clock

Clocks are Not Perfect: Clock Skew



You Can Have Two Types of Skew!



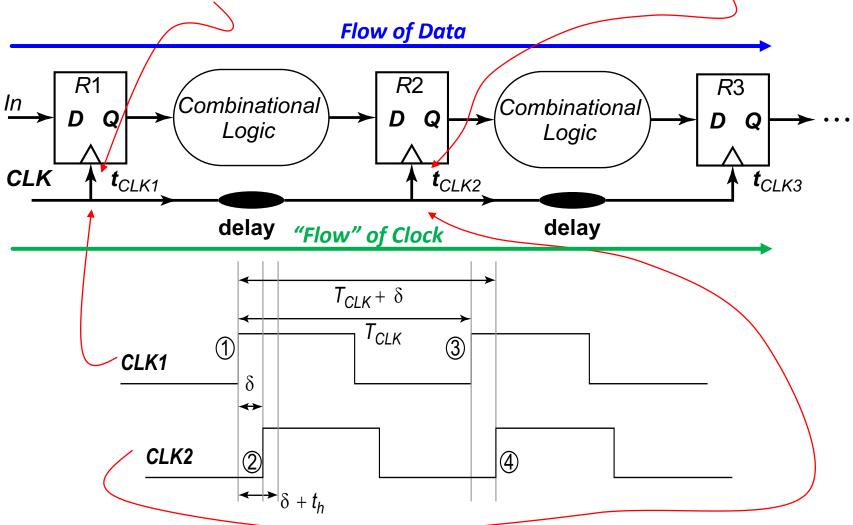


>Adapted from J. Rabaey, A. Chandrakasan, B. Nikolic,

[&]quot;Digital Integrated Circuits: A Design Perspective" Copyright 2003 Prentice Hall/Pearson.

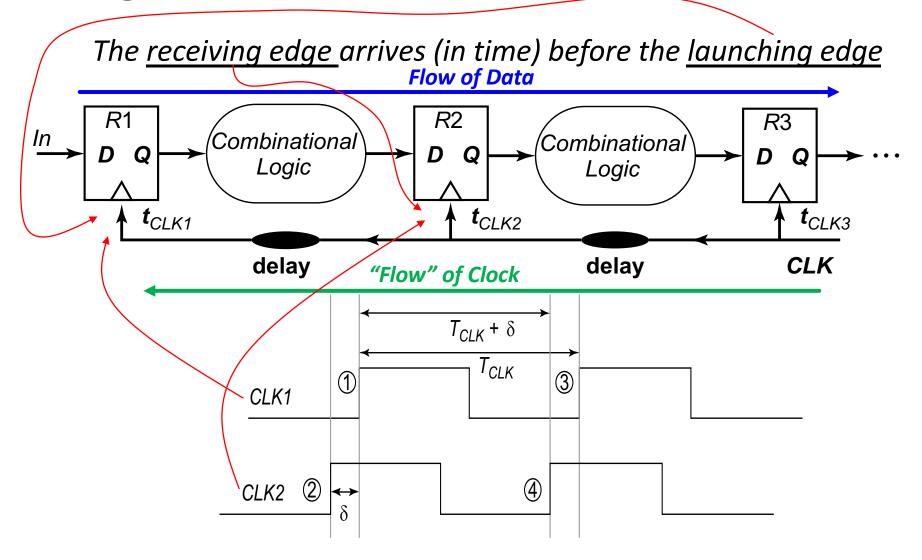
Positive Skew

The <u>launching edge</u> arrives (in time) before the <u>receiving edge</u>



Adapted from J. Rabaey, A. Chandrakasan, B. Nikolic,

Negative Skew



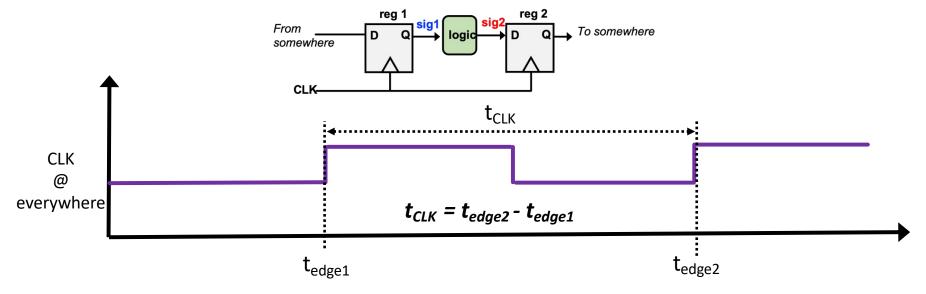
>Adapted from J. Rabaey, A. Chandrakasan, B. Nikolic,

[&]quot;Digital Integrated Circuits: A Design Perspective" Copyright 2003 Prentice Hall/Pearson.

Timing From somewhere CLK-=determined state $t_{\text{CLK}} \\$ =undetermined state CLK $t_{\text{PD,reg1}}$ \geq t_{SETUP,reg2} t_{CD,reg1}◆▶ sig1 ► t_{PD,logic} \geq t_{HOLD,reg2} sig2 t_{CD,logic} ◆ time $t_{PD,reg1} + t_{PD,logic} + t_{SETUP,reg2} \le t_{CLK}$ Two Requirements/ **Conclusions:** $t_{CD,reg1} + t_{CD,logic} \ge t_{HOLD,reg2}$

How does Skew Affect Those Equations?

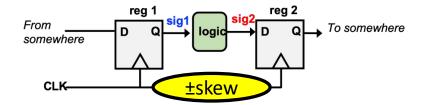
 Originally in our model circuit, we assume all devices experience the clock edges at the same time!!!!!

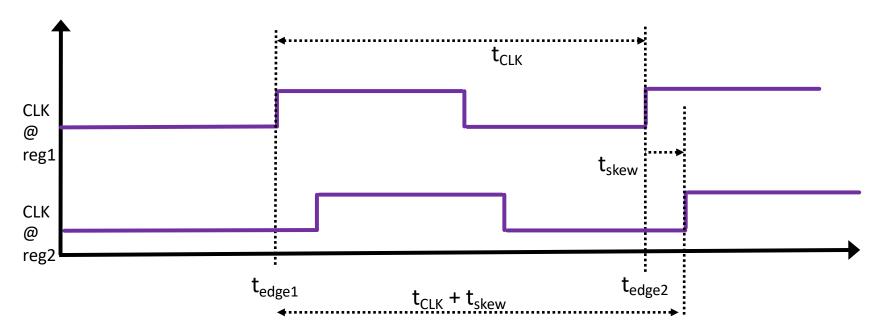


- The Setup equation: $t_{PD,reg1} + t_{PD,logic} + t_{SETUP,reg2} \le t_{CLK}$
- ...was really short-hand for:

$$\frac{t_{edge1}}{t_{edge1}} + t_{PD,reg1} + t_{PD,logic} + t_{SETUP,reg2} \le \frac{t_{edge2}}{t_{edge2}}$$

With Skew in the Mix...





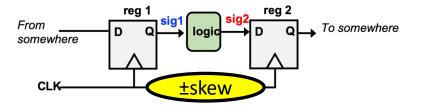
The equation turns into:

$$t_{edge1} + t_{PD,reg1} + t_{PD,logic} + t_{SETUP,reg2} \le t_{edge2} + t_{skew}$$

• But since $t_{CLK} = t_{edge2} - t_{edge1}$

$$t_{PD,reg1} + t_{PD,logic} + t_{SETUP,reg2} \le \frac{t_{clk}}{t_{clk}} + t_{skew}$$

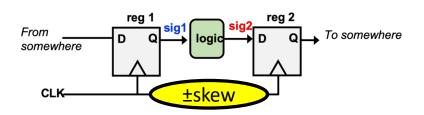
With Skew



$$t_{PD,reg1} + t_{PD,logic} + t_{SETUP,reg2} \le \frac{t_{clk}}{t_{clk}} + t_{skew}$$

- If that's now our modified setup equation...
 - Positive skew makes equation easier to satisfy
 - Negative skew makes equation harder to satisfy
- It can still be fixed even in negative skew case
 - <u>BUT</u> you have degree of freedom with $t_{PD,logic}$...maybe you can change that?
 - <u>AND/OR</u> you could also increase t_{clk} as well.

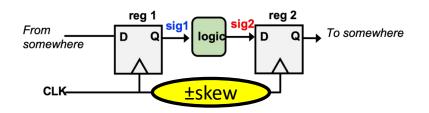
What about Hold Time?



- If the second register is getting its clock edge t_{skew} after the first register that means it needs hold the values at the input of reg2 for t_{skew} longer
- Hold Equation gets modified to be :-/

$$t_{CD,reg1} + t_{CD,logic} \ge t_{HOLD,reg2} + t_{skew}$$

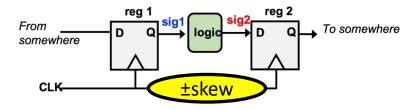
What about Hold Time?



$$t_{CD,reg1} + t_{CD,logic} \ge t_{HOLD,reg2} + t_{skew}$$

- The "growth" from positive skew is not on low side of inequality so...
- Positive skew makes equation harder to satisfy.
 - Further there's nothing you can do since contamination delays are usually very low and beyond our control
- Negative skew makes equation easier to satisfy.

Conclusions



$$t_{PD,reg1} + t_{PD,logic} + t_{SETUP,reg2} \le t_{clk} + t_{skew}$$
 $t_{CD,reg1} + t_{CD,logic} \ge t_{HOLD,reg2} + t_{skew}$

- Positive clock skew improves the minimum cycle time of our design but makes it harder to meet register hold times.
- Negative clock skew hurts the minimum cycle time of our design but makes it easier to meet register hold times.
- Positive skew is tougher to deal with

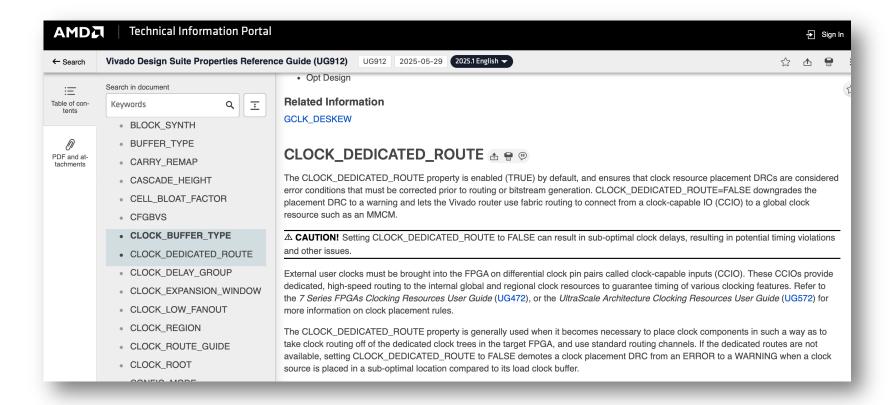
Low-skew Clocking in FPGAs

 When Vivado is doing place-and-route it tries to position logic so that skew is minimized wherever possible

 Special clock paths and buffers exist throughout the chip to distribute the clock as effectively as possible.

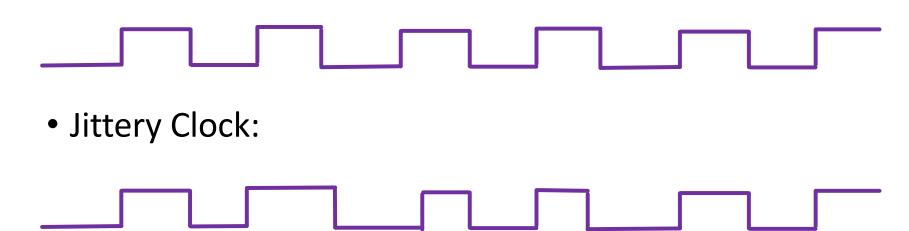
Think of it like priority boarding/VIP status for signals

From the Vivado Docs



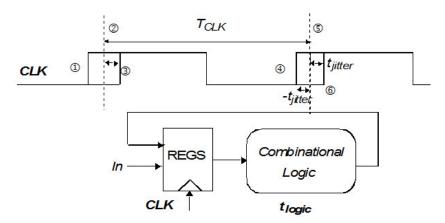
Other Problems you can have with clocks...

• Stable Clock:



Clock jitter means cycle-to-cycle you can have larger or shorter clock periods!

Clocks Are Not Perfectly Periodic!:



- Jitter is an approximation of how much the clock period can increase/decrease cycle to cycle:
- Can make it harder to meet timing since it effectively shortens t_{clk} ...
- Even though some cycles might have larger tclk, we, as engineers are required to be big pessimists and plan for the worst case at all times...
- and that affects the setup equation...

$$t_{PD,reg1}+t_{PD,logic}+t_{SETUP,reg2} \le t_{CLK}-2t_{jitter}$$

Typical crystal oscillator 100mhz (10ns) Jitter: 1ps

Other Problems you can have with clocks...

• 50% Duty Cycle Clock



Not 50% Duty Cycle Clock



What is the clock period of the 50% duty cycle clock vs the non-50% duty cycle clock?

Trick question: they're the same. I got you.

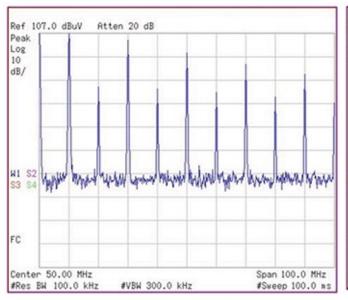
So What? Fifty Shmifty

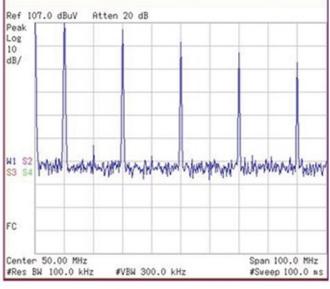
- Even though the clock period is the same, there can be issues.
- In more advanced designs, you use both clock edges (timing gets more complicated). 50% duty cycle ensures equal time for both halves of logic
- Too far of a deviation from 50% may also break the setup/hold time model of our flip-flops
 - Most flip flops have minimium-pulse duration specs...go too low and they won't react appropriately.

Also 50% is "Pure"



- A pure 50% Duty cycle signal has no odd harmonics*
- Non 50% duty cycle will have odd harmonics, so you can get more noise





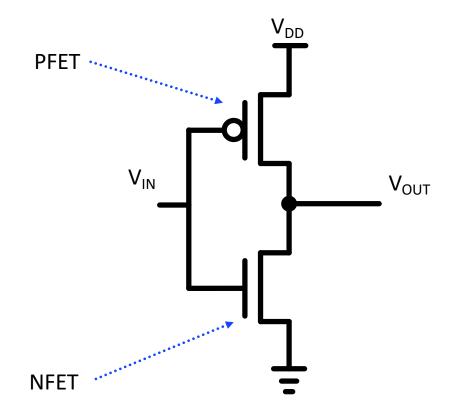
*Take 6.300

Almost All Modern Digital Design is CMOS:

• PFET in charge of making signal go to 1.

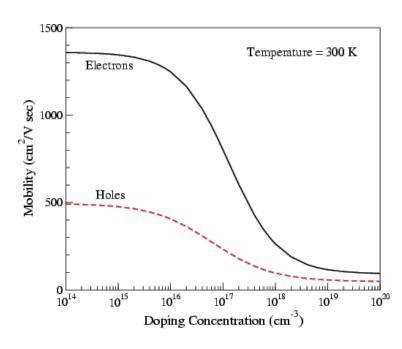
• NFET in charge of making signal go to 0.

They work in a
 <u>C</u>omplementary fashion



Device Physics is Hard* (6.2080, 6.2090, 6.6400, etc...)

- The electrons and holes that N- and P- channel devices use are uneven in mobility so it is very hard to make exactly balanced N- and P- channel FETS
- They may pull to 1 and pull to 0 with different "strengths"
- Very easy for circuits to quickly deviate from equal time in on and off state!

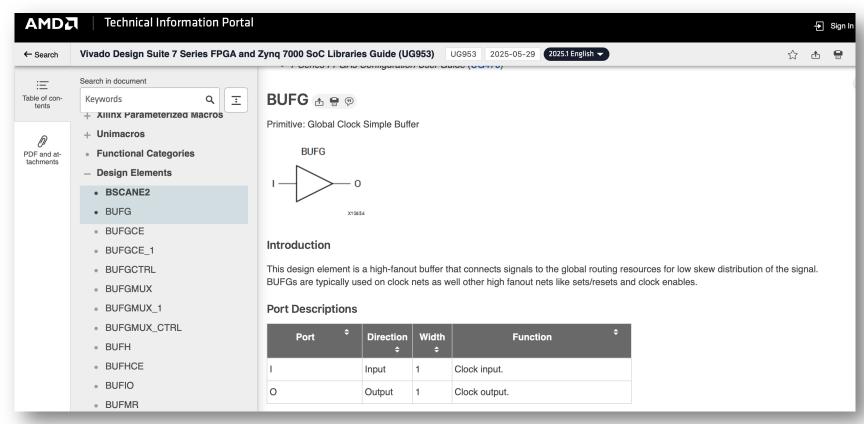


https://www.iue.tuwien.ac.at/phd/park/node30.html

*but fun and fulfilling

Duty Cycle

 Driving clocks with healthy circuits that get some daily exercise is important



And Other Special Circuits

 Other Special Circuits like Phase-Locked Loops help designs keep healthy, clean 50% duty cycle clocks with low jitter

 They can also be used to make clocks from other clocks!

Goal: Use as few clock domains as possible

Suppose we have a reference clk at frequency f and we want signals at f/2, f/4, f/8, etc.:????

```
logic clk2,clk4,clk8,clk16;
always_ff @(posedge clk)begin
    clk2 <= ~clk2:
end
always_ff @(posedge clk2)begin
    clk4 <= ~clk4:
end
always_ff @(posedge clk4)begin
    clk8 <= ~clk16:
end
always_ff @(posedge clk8)begin
    clk16 <= ~clk16;
end
```

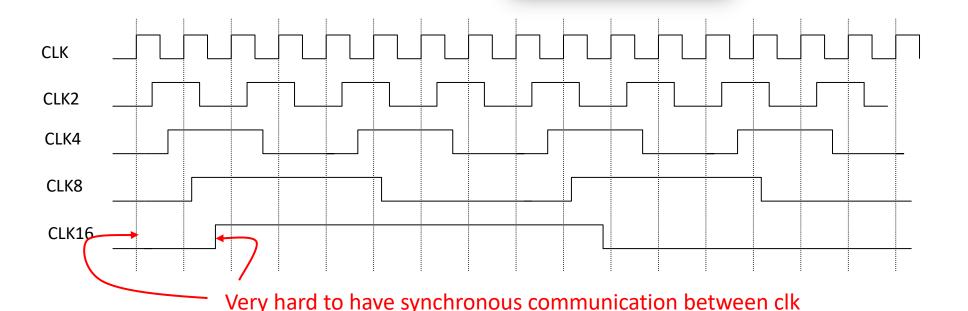
Goal: use as few clock domains as possible

Suppose we have a reference clk at frequency f and we want signals at f/2, f/4, f/8, etc.:????

```
logic clk2,clk4,clk8,clk16;

always_ff @(posedge clk)begin
    clk2 <= ~clk2;
end
    always_ff @(posedge clk2)begin
     clk4 <= ~clk4;
end
    always_ff @(posedge clk4)begin
     clk8 <= ~clk16;
end
    always_ff @(posedge clk8)begin
     clk16 <= ~clk16;
end</pre>
```

No! don't do it this way, you'll never make a dime



and clk16 domains... Can lead to lots of timing violations!

Goal: Use as few clock domains as possible

Suppose we have a reference clk at frequency f and we want signals at f/2, f/4, f/8, etc.:????

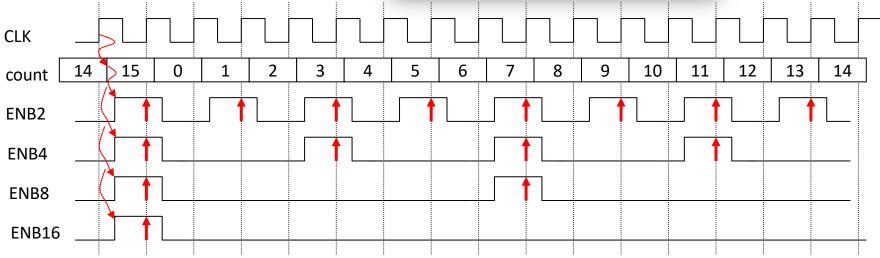
```
logic [3:0] count;
always ff @(posedge clk) begin
    count \leftarrow count + 1; // counts 0..15
end
logic enb2, enb4, enb8, enb16;
assign enb2 = (count[0] == 1'b1);
assign enb4 = (count[1:0] == 2'b11);
assign enb8 = (count[2:0] == 3'b111);
assign enb16 = (count[3:0] == 4'b1111);
always_ff @(posedge clk) begin
  if (enb2) begin
    // get here every 2nd cycle
  end
end
```

Solution: <u>One</u> clock, Many enables

Use one (high speed)
 clock, but create enable
 signals to select a
 subset of the edges to
 use for a particular
 piece of sequential logic
 (much easier on timing
 requirements)

```
logic [3:0] count;
always_ff @(posedge clk) begin
    count <= count + 1;  // counts 0..15
end
logic enb2, enb4, enb8, enb16;
assign enb2 = (count[0] == 1'b1);
assign enb4 = (count[1:0] == 2'b11);
assign enb8 = (count[2:0] == 3'b111);
assign enb16 = (count[3:0] == 4'b1111);
always_ff @(posedge clk) begin
    if (enb2) begin
    // get here every 2nd cycle
    end
end</pre>
```

Yes! A good idea that will lead to good outcomes

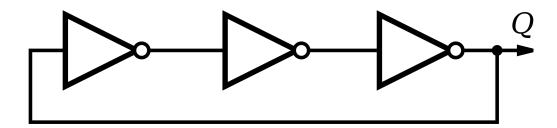


= clock edge selected by enable signal

How to Make Frequencies and Clocks

Where do they come from???

Where do we get frequencies?



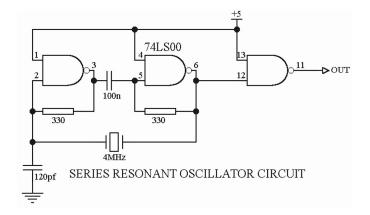
- Particular combinational circuits that are fed back onto themselves so that they cannot be stable can be made to form oscillators.
- The ring oscillator above is a classic example.
- There is no stable set of output states so this circuit perpetually oscillates.
- Period of oscillation is based on the delay of each element

Where do we get frequencies?

- Most frequencies come from Crystal Oscillators made of quartz
- Equivalent to very High-Q RLC tank circuits
- Incorporate into circuit like that below and boom, you've got a square wave of some specified frequency dependent largely on the crystal



16MHz Crystal



High Frequencies

 Very hard to get a crystal oscillator to operate above ~200 MHz (7th harmonic of resonance of crystal itself, which usually is limited to about 30 MHz due to fabrication limitations)

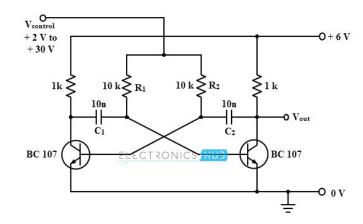
 Where does the 2.33 GHz clock of my iPhone come from then?

Frequency Multipliers!

Voltage Controlled Oscillator

- It is very easy to make voltagecontrolled oscillators that run up to 1GHz or more.
 - Low voltage circuit oscillates at low frequency
 - Higher voltage → higher frequency oscillation
- Block Diagram:





A simple VCO (not type found in FPGA). Same general idea... You use **FEEDBACK** to make a circuit unstable but guide that instability into productive oscillations with careful tuning and external control!

Voltage Controlled Oscillator

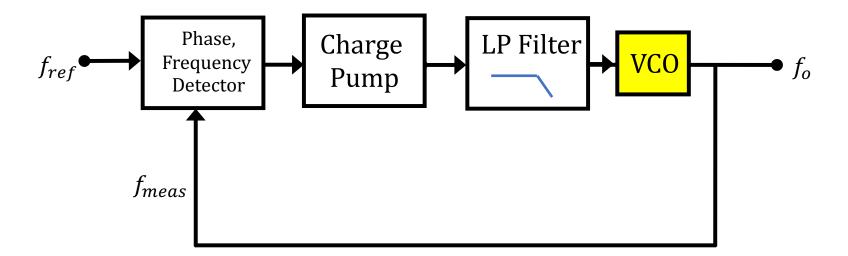
- It is very easy to make voltage-controlled oscillators that run up to several GHz or more.
- Why don't we just:



- Pick the voltage V_i that is needed to get the frequency we want f_o ?
- That's gotta be ok right?

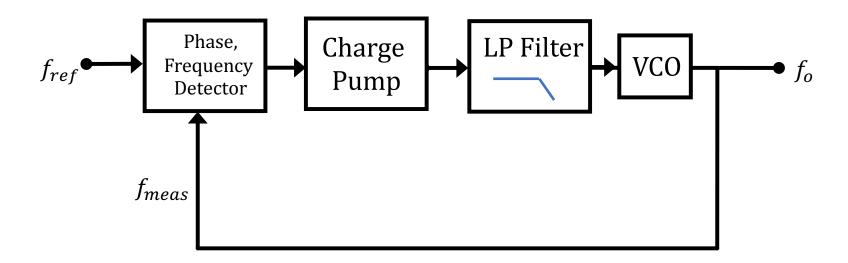
Phase Locked Loop (PLL)

• Place the unstable, but capable, VCO in a feedback loop.



Phase Locked Loop (PLL)

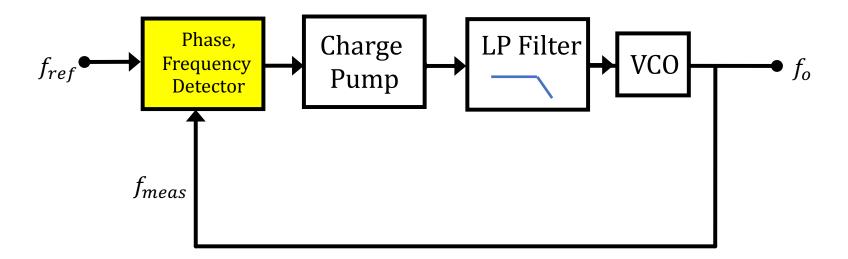
• A PLL is a circuit that can track an input frequency f_{ref} of a system and reproduce it at the output f_o



GOTTA GO THROUGH EACH PART

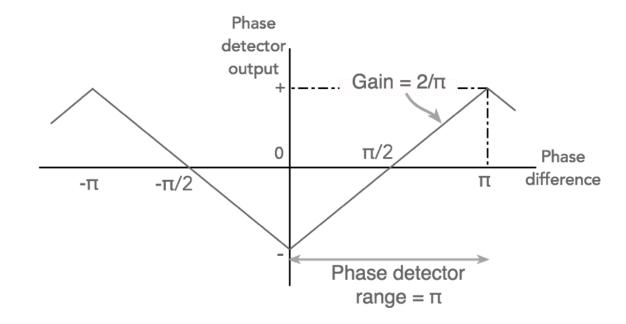
Phase Locked Loop (PLL)

• The Phase, Frequency Detector

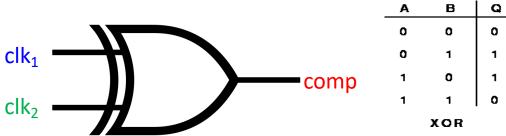


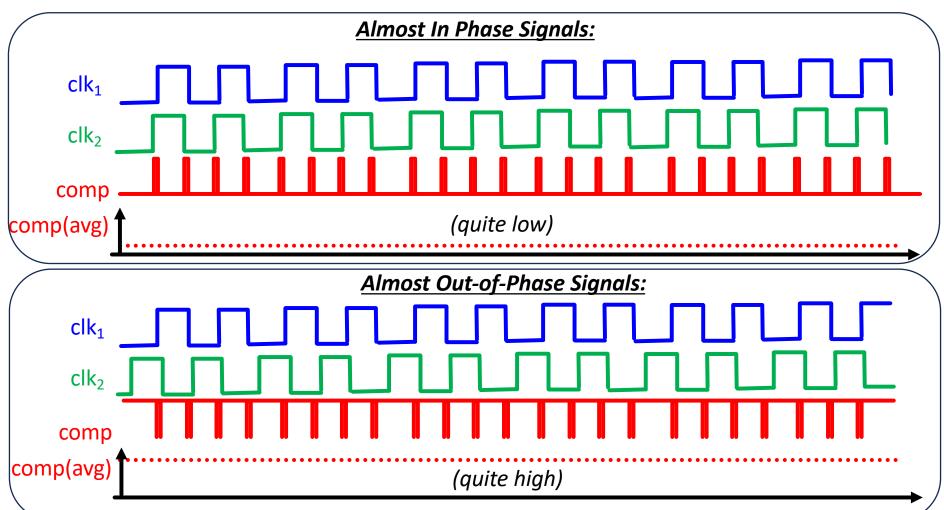
Phase Detector

- Can be a simple XOR, XNOR gate
 - Low-pass the output



Phase Detector...

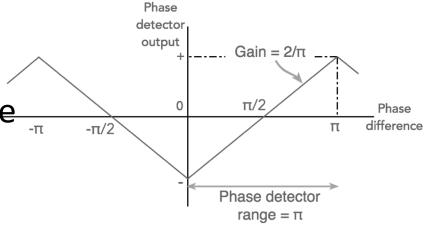




Phase Detector

Can be a simple XOR, XNOR gate

Low-pass the output

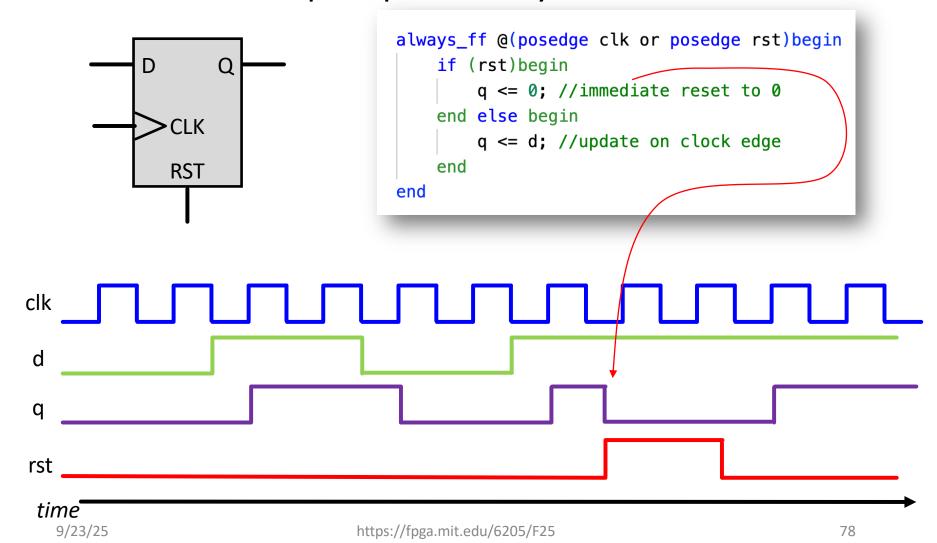


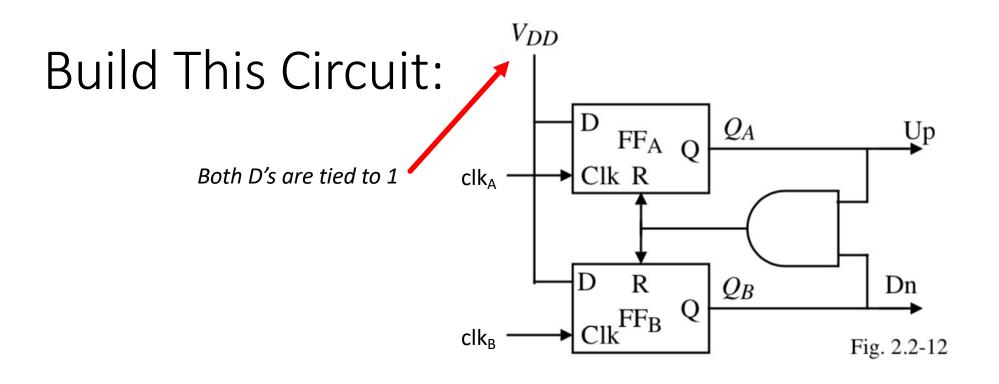
 If near the desired frequency already this can work...if it is too far out, it won't and can be very unreliable since phase and frequency are related but not quite the same thing, it will lock onto harmonics, etc...

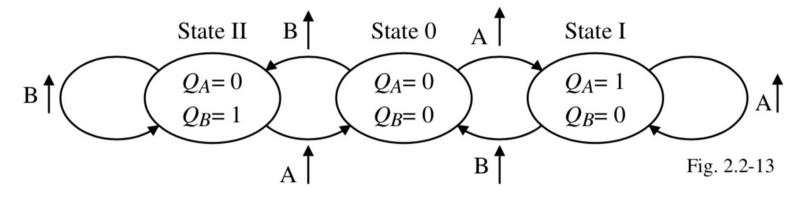
- For frequency we instead use a PFD:
 - Phase/Frequency Detector:

Phase-Frequency Detection

Built around Flip-Flops with Asynchronous Resets:

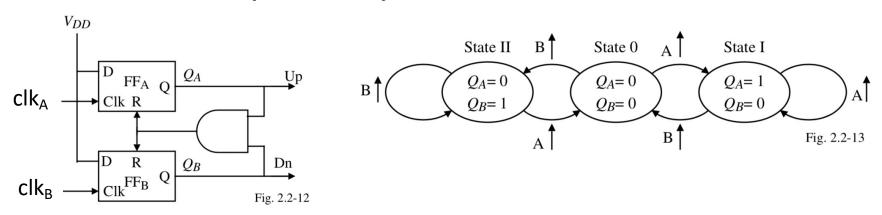






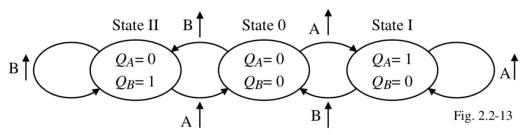
1.pallen.ece.gatech.edu/Academic/ECE_6440/Summer_2003/L070-DPLL(2UP).pdf

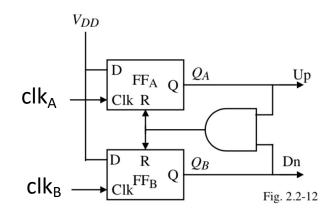
Phase Frequency Detection



- Circuit starts in State 0 (middle) ("Up" off, "Dn" off)
- First clock to rise will move into one of two side states:
 - clk_A?: State 1 ("Up" on, "Dn" off)
 - clk_B?: state II ("Dn" on, "Up" off)
- When loser finally rises, circuit resets to State 0 (middle)
- Competition starts again

Phase Frequency Detection

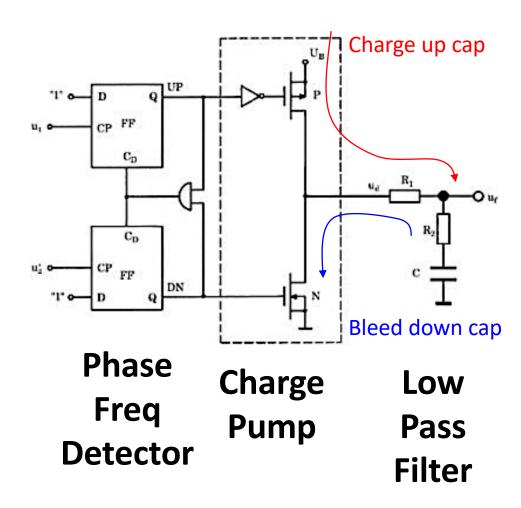




- If clk_A is higher frequency, it will, on average, win more races and the FSM will spend more time in State I
- If clk_B is higher frequency, it will, on average, win more races and the FSM will spend more time in State II
- The closer they are, the more balanced the State I and State II time will be
- The greater their difference, the greater the on-average discrepency

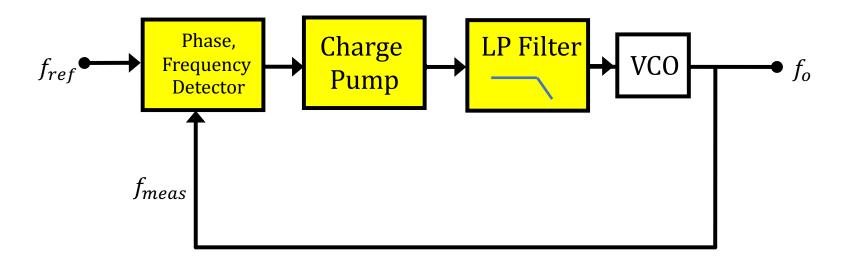
UP and DN control a capacitor voltage

- If you're in State I:
 - Increase voltage on capacitor
- If you're in State II:
 - Decrease voltage on capacitor
- The voltage that builds up will be tightly related to how different these two clocks are



Phase Locked Loop (PLL)

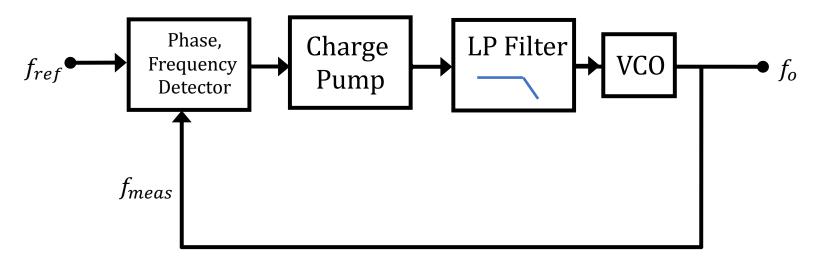
So that's those three pieces



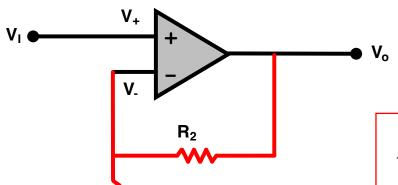
Phase Locked Loop (PLL)

- So this circuit can make $f_0 = f_{ref}$ and there's lots of uses for this (frequency locking, etc...)
 - But that doesn't help us! I want higher frequencies. You said we could do that.
 - I feel betrayed and angry and don't know how to express that emotion in a healthy way

How can we make a higher frequency?



Use Resistors in Voltage Divider in Feedback Path!



 A voltage divider in feedback path gives us voltage gain!

$$K=rac{1}{1-p+G}$$
 $p pprox 0.9999$ means $K=rac{1}{G}$
$$G=rac{R_1}{R_1+R_2}$$

The gain A_{v} of this circuit is therefore:

$$V_{-} = V_{o} \frac{R_{1}}{R_{1} + R_{2}}$$

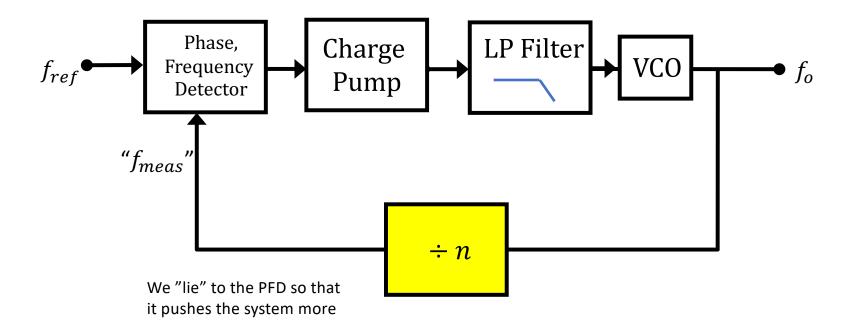
$$A_v = \frac{R_1 + R_2}{R_1}$$

The gain of a "non-inverting amplifier"

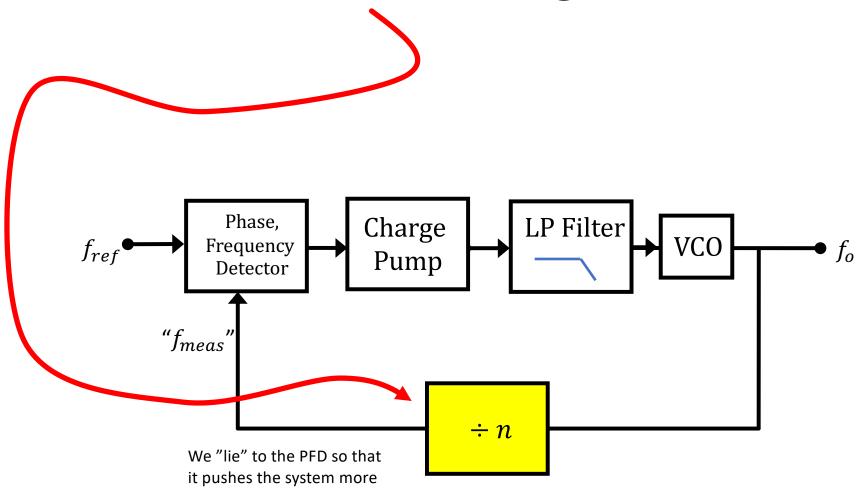
Same Idea with Phase Locked Loops!

Use a Clock Divider in Feedback Path!

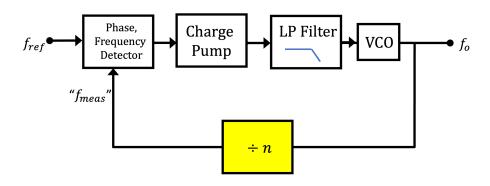
- A clock divider in feedback path gives us clock gain!
- By lying to the circuit, you can emotionally manipulate the system as a whole to make higher, stable frequencies.



Where is that coming from?



Can actually just use flip-flops to divide

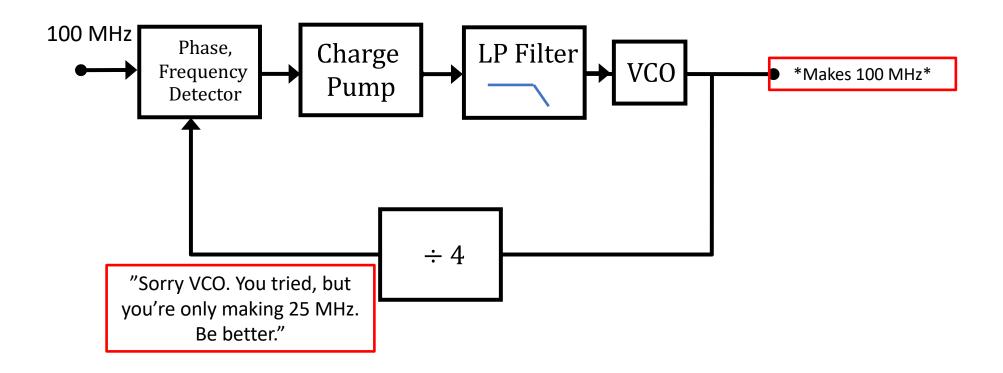


 The PFD will handle the phase mismatch that arises from the propagation delays naturally

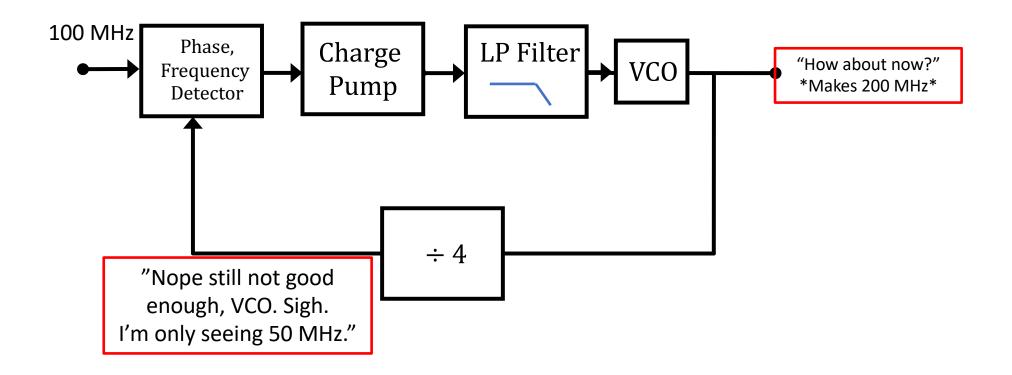
```
logic clk2,clk4,clk8,clk16;

always_ff @(posedge clk)begin
    clk2 <= ~clk2;
end
always_ff @(posedge clk2)begin
    clk4 <= ~clk4;
end
always_ff @(posedge clk4)begin
    clk8 <= ~clk16;
end
always_ff @(posedge clk8)begin
    clk16 <= ~clk16;
end</pre>
```

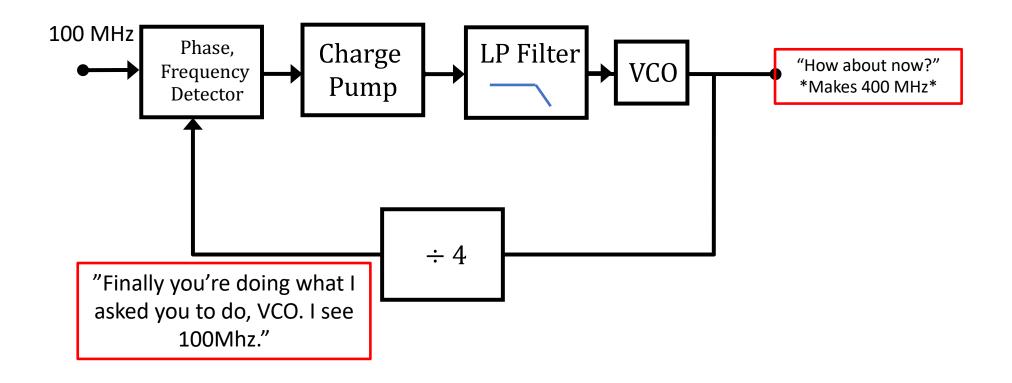
Example of a Toxic Relationship Circuit



Example of a Toxic Relationship Circuit



Example of a Toxic Relationship Circuit

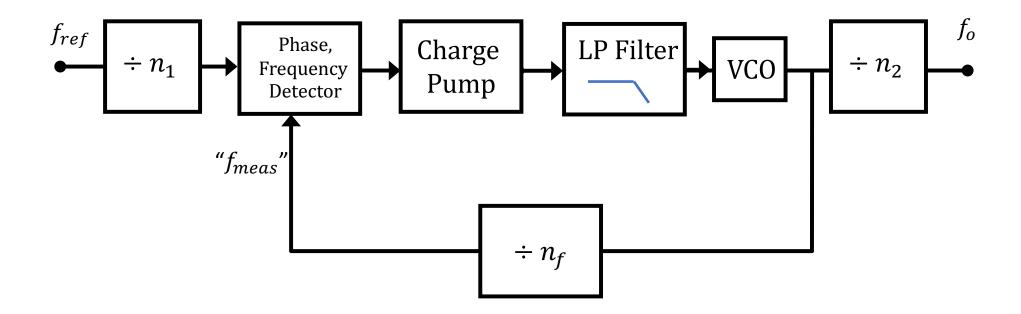


Conclusions

- Do not be in emotionally manipulative friendships or work-relationships, regular relationships. You are better than that.
- Do not emotionally manipulate other people.
- Circuits are not people so it is probably ok and can be beneficial.
- Negative fractional feedback in PLLs allows us to generate higher frequencies that are stable since they are referenced to lower (stable) frequency sources.

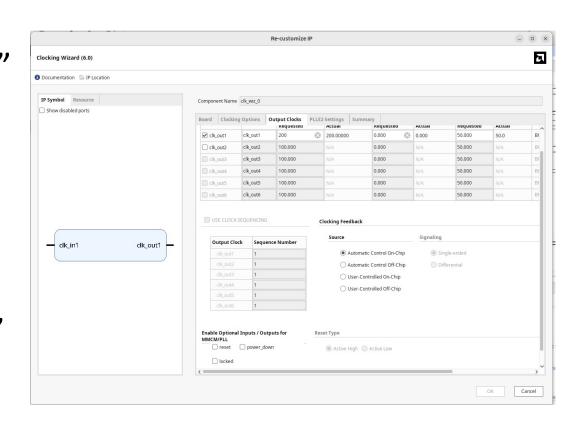
Add a Pre- and Post- Divider for Flex

 There will often be additional stages of frequency division to improve flexibility and range



Do we/I have to build this?

- Yes/No. Circuit is too sensitive for us to specify details in Verilog on an FPGA
- Most FPGAs have pre-built "hardened" Mixed-Mode Clock Management (MMCM) units and PLLs to deploy
- You can configure them with "wizards"



In Week 04

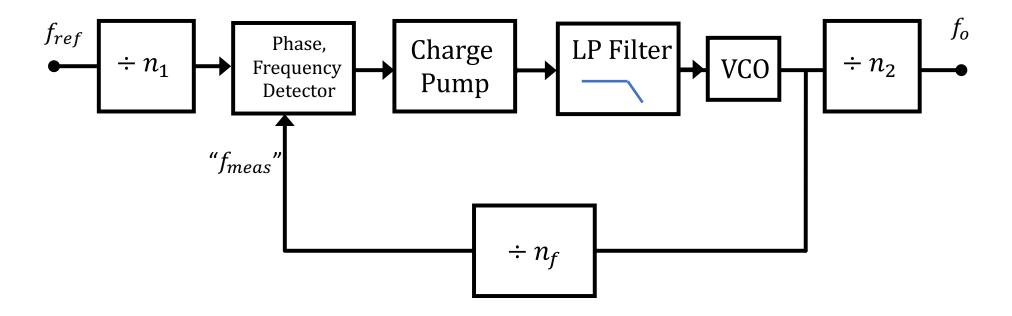
- We'll build HDMI video from scratch.
- For 720p we'll need:
- a clock at 74.25 MHz (for the pixels)
- A clock at 371.25 MHz (for the bits of the pixels to be sent serially)
 - We'll use this clock along with a device that is built to run using always @(posedge clk or negedge clk) to get 742.25 MHz of data out to drive the 720p data.

So to Make 74.25 MHz and 371.25 MHz?

Instance of clock manager:

```
MMCME2 ADV
#(.BANDWIDTH
                        ("OPTIMIZED").
  .CLKOUT4_CASCADE
                        ("FALSE"),
                        ("ZHOLD"),
  .COMPENSATION
                                           2. Divides by 5
                        ("FALSE")
  STARTUP WAIT
  .DIVCLK_DIVIDE
                        (5)
                                               3. Multiplies by 37.125
  .CLKFBOUT_MULT_F
                        (37.125)
  .CLKFBOUT_PHASE
                        (0.000),
  .CLKFBOUT_USE_FINE_PS ("FALSE"),
                                               4a. Divide by 10 for 74.25 MHz
  .CLKOUTØ DIVIDE F
                        (10.000)
  .CLKOUT0 PHASE
                        (0.000)
  .CLKOUTO DUTY CYCLE
                        (0.500).
  .CLKOUT0_USE_FINE_PS
                        ("FALSE"),
                                          4b. Divide by 2 for 371.25 MHz
  .CLKOUT1 DIVIDE
                        (2)
  .CLKOUT1 PHASE
                        (0.000).
  .CLKOUT1_DUTY_CYCLE
                        (0.500),
  .CLKOUT1_USE_FINE_PS
                        ("FALSE"),
  .CLKIN1_PERIOD
                        (10.000))
                                              1. Takes in 100 MHz
mmcm_adv_inst
  // Output clocks
```

Side-Note



• n_f and n_2 can generally be fractions by switching between several dividers with a time-weighted averaging

Timing in Vivado

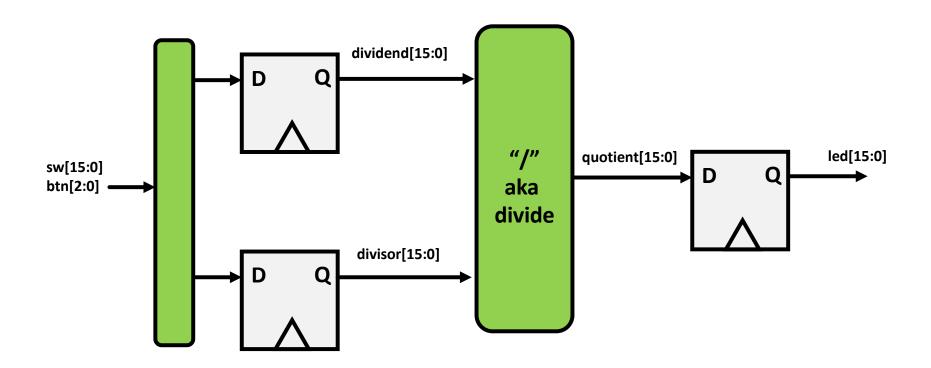
Starting to Look

Let's Look at Some Code:

- Very Simple top_level:
- Use sw[15:0] and buttons to seed two values into 16 bit registers:
 - Dividend
 - Divisor
- When btn[0] is pushed:
 - DIVIDE the 16 bit numbers

```
timescale 1ns / 1ps
`default nettype none
module top level(
       input wire clk 100mhz, //clock @ 100 mhz
       input wire [15:0] sw, //switches
       input wire [3:0] btn, //all four momentary button switches
       output logic [15:0] led //just here for the funs
);
  logic [3:0] old btn;
  logic [15:0] guotient;
  logic [15:0] dividend;
  logic [15:0] divisor:
  assign led = quotient;
  always_ff @(posedge clk_100mhz)begin
    for (int i=0; i<4; i=i+1)begin
      old btn[i] <= btn[i]:
  always ff @(posedge clk 100mhz)begin
    if (btn[0] & ~old btn[0])begin
      quotient <= dividend/divisor; //divide</pre>
    end
    if (btn[1] & ~old_btn[1])begin
      dividend <= sw; //divide //load dividend</pre>
    end
    if (btn[2] & ~old btn[2])begin
      divisor <= sw; //divide //load dividend</pre>
    end
  end
endmodule
`default_nettype wire
```

What does this build



Let's Build it.

Terminal Output:

```
jodalyst@Josephs-MBP lec06 % ./remote/r.py build.py build.tcl hdl/* xdc/* obj
...
...
Writing bitstream obj/final.bit...
INFO: [Vivado 12-1842] Bitgen Completed Successfully.
INFO: [Project 1-1876] WebTalk data collection is mandatory when using a ULT device.
To see the specific WebTalk data collected for your design, open the
usage_statistics_webtalk.html or usage_statistics_webtalk.xml file in the
implementation directory.
INFO: [Common 17-83] Releasing license: Implementation
7 Infos, 0 Warnings, 0 Critical Warnings and 0 Errors encountered.
write_bitstream completed successfully
write_bitstream: Time (s): cpu = 00:00:04; elapsed = 00:00:14 . Memory (MB): peak =
2729.707; gain = 206.934; free physical = 2837; free virtual = 8407
```

"Hmmm Looks good."



"Jeeze when I deploy this in a high-throughput system where I have a new pair of numbers to divide every 10ns, the division results are trash. Oh well it must be a failure of the FPGA or literally anything other than things that I have done. Gonna ask for the checkoff."

Quote overheard in lab.

You look through the output from the build...

Starting at line 1322:

```
Verification completed successfully
Phase 20 Verifying routed nets | Checksum: 12923a084
Time (s): cpu = 00:00:12; elapsed = 00:00:13. Memory (MB): peak = 2520.699; qain = 0.000; free
physical = 3116 ; free virtual = 8674
Phase 21 Depositing Routes
Phase 21 Depositing Routes | Checksum: 14a6fdc22
Time (s): cpu = 00:00:12; elapsed = 00:00:13. Memory (MB): peak = 2520.699; qain = 0.000; free
physical = 3116; free virtual = 8674
Phase 22 Post Router Timing
INFO: [Route 35-20] Post Routing Timing Summary | WNS=-21.399| TNS=-129.552| WHS=0.090 | THS=0.000
Phase 22 Post Router Timing | Checksum: 1a0e6c79b
Time (s): cpu = 00:00:12; elapsed = 00:00:13. Memory (MB): peak = 2520.699; qain = 0.000; free
physical = 3116; free virtual = 8674
CRITICAL WARNING: [Route 35-39] The design did not meet timing requirements. Please run
report_timing_summary for detailed reports.
Resolution: Verify that the timing was met or had small violations at all previous steps (synthesis,
placement, power_opt, and phys_opt). Run report_timing_summary and analyze individual timing paths.
INFO: [Route 35-253] TNS is the sum of the worst slack violation on every endpoint in the design. Review
the paths with the biggest WNS violations in the timing reports and modify your constraints or your
design to improve both WNS and TNS.
INFO: [Route 35-16] Router Completed Successfully
Phase 23 Post-Route Event Processing
Phase 23 Post-Route Event Processina | Checksum: 3725a886
Time (s): cpu = 00:00:12; elapsed = 00:00:13 Memory (MB): peak = 2520.699; gain = 0.000; free physicol = 3116: free virtual = 8674 https://fpga.mit.edu/6205/F25
                                                                                                        103
physical = 3116; free virtual = 8674
```

Look at

post_route_timing.rpt

```
Timing Report
Slack (VIOLATED) :
                            -21.399ns (required time - arrival time)
  Source:
                            dividend_reg[15]/C
                              (rising edge-triggered cell FDRE clocked by gclk {rise@0.000ns fall@4.000ns period=10.000ns})
  Destination:
                            quotient_rea[0]/D
                              (rising edge-triggered cell FDRE clocked by gclk {rise@0.000ns fall@4.000ns period=10.000ns})
  Path Group:
                            Setup (Max at Slow Process Corner)
  Path Type:
                            10.000ns (gclk rise@10.000ns - gclk rise@0.000ns)
31.483ns (logic 21.642ns (68.742%) route 9.841ns (31.258%))
  Requirement:
  Data Path Delay:
                            82 (CARRY4=80 LUT2=1 LUT3=1)
  Logic Levels:
  Clock Path Skew:
                            0.026ns (DCD - SCD + CPR)
    Destination Clock Delay (DCD):
                                         4.926ns = (14.926 - 10.000)
    Source Clock Delay
                              (SCD):
                                         5.079ns
    Clock Pessimism Removal (CPR):
                                         0.179ns
  Clock Uncertainty:
                            0.035ns ((TSJ<sup>2</sup> + TIJ<sup>2</sup>)<sup>1</sup>/2 + DJ) / 2 + PE
    Total System Jitter
                              (TSJ):
                                         0.071ns
    Total Input Jitter
                                         0.000ns
                              (TIJ):
    Discrete Jitter
                               (DJ):
                                         0.000ns
    Phase Error
                               (PE):
                                         0.000ns
```

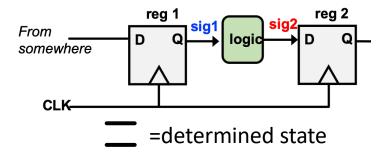
What is Slack?

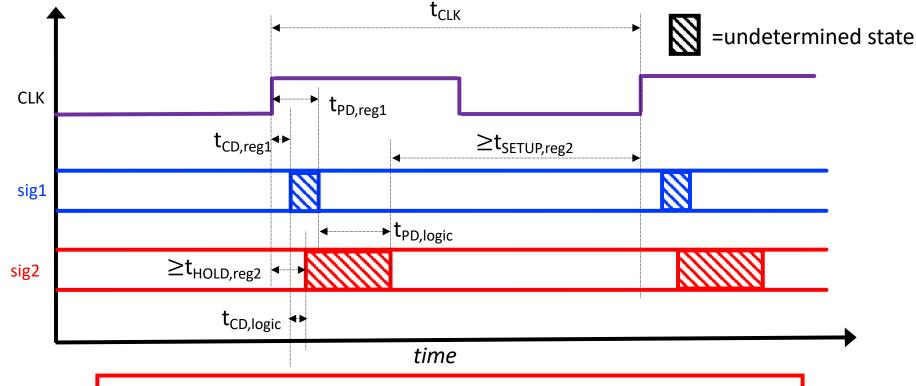
- Slack: measure of how safe your timing is
- The two big timing constraints we worry about are related to setup and hold
- Therefore there are two Slack values:
 - Setup slack: t_{required} t_{actual}
 - Hold slack: t_{actual} t_{required}

These are defined such that:
Positive is **GOOD** ©
Negative is **BAD** Ø

Timing Diagram

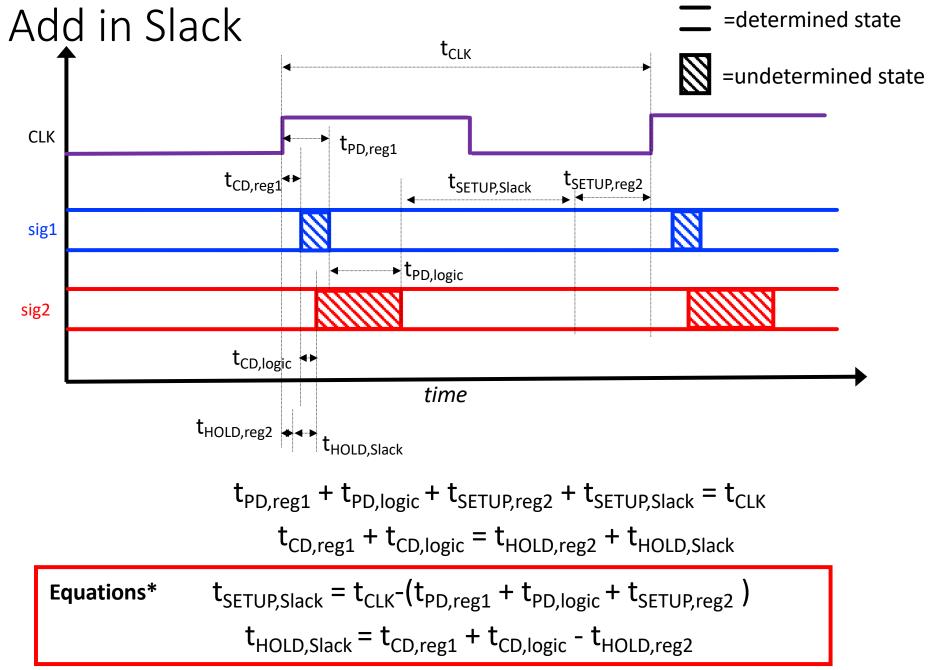
This thing again. Unbelievable, it is almost like this diagram is important or something





Two Requirements/Conclusions:

$$\begin{aligned} t_{\text{PD,reg1}} + t_{\text{PD,logic}} + t_{\text{SETUP,reg2}} &\leq t_{\text{CLK}} \\ t_{\text{CD,reg1}} + t_{\text{CD,logic}} &\geq t_{\text{HOLD,reg2}} \end{aligned}$$



Conclusion

- Positive Slack is GOOD
- Negative Slack is BAD

Look at

This is not good Negative Slack

routerpt report timing.rpt

```
Timing Report
Slack (VIOLATED) :
                          -21.399ns (required time - arrival time)
                          dividend_reg[15]/C
  Source:
                            (rising edge-triggered cell FDRE clocked by gclk {rise@0.000ns fall@4.000ns period=10.000ns})
  Destination:
                          auotient reaΓ01/D
                            (rising edge-triggered cell FDRE clocked by gclk {rise@0.000ns fall@4.000ns period=10.000ns})
  Path Group:
                          aclk
                          Setup (Max at Slow Process Corner)
  Path Type:
                          10.000ns (gclk rise@10.000ns - gclk rise@0.000ns)
  Requirement:
                          31.483ns (logic 21.642ns (68.742%) route 9.841ns (31.258%))
  Data Path Delay:
  Logic Levels:
                          82 (CARRY4=80 LUT2=1 LUT3=1)
  Clock Path Skew:
                          0.026ns (DCD - SCD + CPR)
    Destination Clock Delay (DOD):
                                      4.926ns = (14.926 - 10.000)
    Source Clock Delay
                            (SCN):
                                      5.079ns
    Clock Pessimism Removal (CPR):
                                      0.179ns
  Clock Uncertainty:
                          0.035n ((TSJ<sup>2</sup> + TIJ<sup>2</sup>)<sup>1</sup>/2 + DJ) / 2 + PE
    Total System Jitter
                                      0.071ns
                            (TSJ)
    Total Input Jitter
                            (TIJ)
                                      0.000ns
    Discrete Jitter
                             (DJ):
                                      0.000ns
    Phase Error
                             (PE):
                                      0.000ns
                                                                              1/3 from routing
                                 2/3 from routing
```

Results

- By default Vivado only gives you a few offending paths (our default is one) and it provides them in order of worst to best
- You can ask for more paths using different arguments;

https://docs.xilinx.com/r/2025.1-English/ug835-vivado-tcl-commands/report_timing

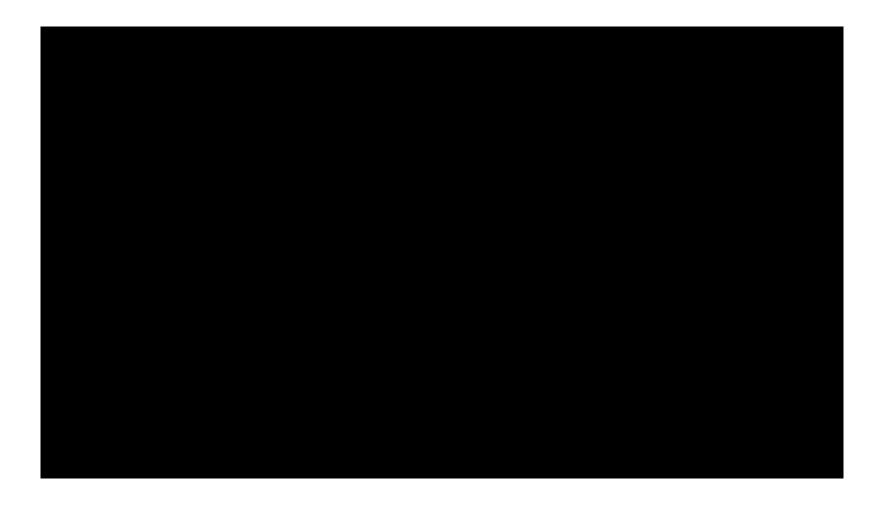
Final Projects Coming Up

• In another ~week or so, we have to start thinking about planning on starting to get going on final projects.

 First part of that is teaming and teams benefit from targeting shared goals

• On the site, we'll put up an archive of final projects

Past Project (with Microphone)



Sudoku Solver

